T-79.148 Autumn 2003

Introduction to Theoretical Computer Science Tutorial 7 Problems

Homework problems:

1. Design a right-linear grammar that generates the language

$$\{w \in \{a,b\}^* \mid w \text{ does not contain substring } bba\}$$

(Cf. Demonstration Problem 3/1b.)

2. (a) Show that the following context-free grammar is ambiguous:

$$\begin{array}{ccc} S & \rightarrow & ASb \mid A \mid b \\ A & \rightarrow & aA \mid a \end{array}$$

- (b) Design an unambiguous grammar for the same language. Describe the language informally.
- 3. Construct a context-free grammar for the language:

$$\{a^i b^j a^k \mid 0 \le i \le j \text{ or } i = k\}$$

Is your grammar ambiguous?

Demonstration problems:

- 4. Prove that the class of context-free languages is closed under unions, concatenations, and the Kleene star operation, i.e. if the languages $L_1, L_2 \subseteq \Sigma^*$ are context-free, then so are the languages $L_1 \cup L_2$, L_1L_2 and L_1^* .
- 5. (a) Prove that the following context-free grammar is ambiguous:

$$S \rightarrow \mathbf{if} \ b \ \mathbf{then} \ S$$

 $S \rightarrow \mathbf{if} \ b \ \mathbf{then} \ S \ \mathbf{else} \ S$
 $S \rightarrow s$

- (b) Design an unambiguous grammar that is equivalent to the grammar in item (a), i.e. that generates the same language. (Hint: Introduce new nonterminals B and U that generate, respectively, only "balanced" and "unbalanced" **if-then-else-**sequences.)
- 6. Design a recursive-descent (top-down) parser for the grammar from Problem 6/6.